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*Geophysical Research Letters*

Supporting Information for

**Identifying sensitive ranges in global warming precipitation change dependence on convective parameters.**

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Text S1  
Figures S1 to S3

**Introduction**

Text S1 and the accompanying figures S1-S3 provide additional details supporting the main text:

- details on simulation set up;
- a demonstration of rapid equilibration as a function of simulation time of a key hydrological cycle measure, showing the case of sensitivity to entrainment across the full feasible range as the case with the largest changes (Text S1 and Fig. S1);
- details on the error bar computations in main text figures Fig. 1 and Fig. 3;
- the December-February precipitation change and precipitation change sensitivities corresponding to Figure. 2 of the main text (Text S1 and Fig. S2);
- examples of CMIP5 archive precipitation change similar to Fig 2a of the main text for reference (Fig. S3).

31 **Text S1.**

32 In this study, simulations of precipitation change under the global warming  
33 Representative Concentration Pathway (RCP) 8.5 scenario, use a branch-run  
34 methodology to minimize spin-up (in CESM technical terms these are hybrid runs  
35 with ocean and sea ice using a restart file and atmosphere/land initialized). Runs  
36 with different parameter settings are restarted from the year 1976 for the  
37 historical period and from 2071 for the end-of-century simulation under RCP 8.5  
38 scenario using a restart files from the standard parameter simulation with the  
39 Community Climate System Model 4 (CCSM4; i.e., a subset of CESM1). This  
40 CCSM4 "restart run" is used only to provide initial conditions; it likewise followed  
41 the CMIP5 historical forcing and RCP8.5 scenario protocol. The standard  
42 parameter CESM1 control is created from an ensemble of runs using this  
43 methodology to have a precise comparison to the parameter perturbation runs in  
44 CESM1. A control ensemble of 15 runs with standard parameter values (CESM1  
45 default values), is created from a set of branch ensemble members each  
46 restarted with initial conditions changed to values from a different year (January  
47 1, 1970-1984 and 2066-2077) in the control run to yield different evolutions of the  
48 internal variability. The year for the analysis is set by the radiative forcing as a  
49 function of time which begins in each case from the same year, 1976 and 2071  
50 respectively. For each of the periods, historical and end-of-century, a 30-year run  
51 is performed (1976-2005 and 2071-2100, respectively), and only last 20 years  
52 are used for the analysis, allowing 10 years for equilibration.

53

54 *Equilibration.*

55 Figure S1 shows an example of the equilibration as a function of time during the  
56 experiment for a measure of one important quantity, the global average  
57 precipitation change across the feasible range in entrainment. Specifically, the  
58 precipitation change for the highest value of entrainment minus that for the  
59 lowest value of entrainment,  $\Delta P_{diff}(t) = \Delta P(\mu_{max}) - \Delta P(\mu_{min})$ , is evaluated as a  
60 function of time  $t$ , where the precipitation change under global warming  $\Delta P$  is  
61 evaluated for an average centered  $t$  years after the start of the end-of-century run  
62 minus the corresponding average  $t$  years after the start of the historical run. The  
63 values  $\mu_{max}$  and  $\mu_{min}$  denote the highest and lowest values of the parameter  $\mu$ , in  
64 this case entrainment. This spatial pattern as a function of time is projected onto  
65 the 30-year average  $\Delta P_{diff\_avg30years}$  which is very similar to the pattern shown in  
66 Fig. 2b. In other words, the measure shown is  $\langle \Delta P_{diff}(t) \cdot \varphi \rangle$  With  
67  $\varphi = \Delta P_{diff\_avg30years} / rms(\Delta P_{diff\_avg30years})$  where angle brackets denote spatial  
68 averaging over the globe. The 20-year averages corresponding to the evaluation  
69 period used in the main text are shown as horizontal bars. The first 2-year  
70 average is close to this value, in other words, a large fraction of the hydrological  
71 cycle response is almost equilibrated within the first two years. Subsequent four-  
72 year averages essentially complete the equilibration, aside from some internal  
73 variability, within the first 10 years. The thickness of the 20-year average bars  
74 indicates  $\pm 1$  standard error for a 20-year average, while the vertical error bars on

75 four-year and two-year averages indicates  $\pm 1$  standard error for these respective  
76 averaging periods.

77

78 *Error bars for figures 1 and 3 in the main text.*

79 Error bars in Fig. 1 of the main text indicate  $\pm 1$  standard error in the estimated  
80 values, i.e. the repeatability of this measure, estimated from the standard  
81 deviation of internal variability for each run. This is estimated by breaking each  
82 run into four-year segments to reduce possible effects of interannual correlation.  
83 The standard deviation across the set of four-year segments, normalized by  $m^{1/2}$ ,  
84 where  $m$  is the number of 4-year segments, is computed for the quantity of  
85 interest,  $rms(P_{exp}-P_{obs})$ , where  $rms$  denotes the spatial root-mean-square,  $P_{exp}$  is  
86 the precipitation simulated for particular experiment and  $P_{obs}$  is observed  
87 precipitation from Global Precipitation Climatology Project. The results for  
88 different parameter value settings were similar and thus are averaged to yield a  
89 single value of the error bar used for each parameter value in Fig. 1.

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91 For Fig. 3 of the main text, the error bars shown are computed using estimates of  
92 internal variability based on the ensemble of 15 runs at control parameter values.  
93 The projection measure  $\langle \Delta P(\mu) \Delta P_{diff} \rangle / rms(\Delta P_{diff})$ , is calculated for each of the 15  
94 runs, and twice the standard deviation of this is used as the error bar for each of  
95 the experiments that has a single run. For the control case, the mean of the 15  
96 runs is displayed with error bars corresponding to a standard error of  $n^{-1/2}$  times  
97 the standard deviation, where  $n=15$  is the number of runs. An alternate  
98 computation of the error bar was also carried out by a method similar to that used  
99 in Fig. 1, i.e. the standard deviation of  $\langle \Delta P(\mu) \Delta P_{diff} \rangle / rms(\Delta P_{diff})$ , of the set of 4-  
100 year segments normalized by  $m^{1/2}$ , where  $m$  is the number of four-year averages,  
101 averaging over all experiments. This yielded error bars very similar to the ones  
102 displayed.

103

104 *December-February precipitation sensitivities.*

105 Figure S2 is the same as Fig. 2, but for December-February, showing spatial  
106 patterns of precipitation change and precipitation change sensitivity across the  
107 feasible range for entrainment, convective timescale, downdraft fraction and  
108 evaporation efficiency.

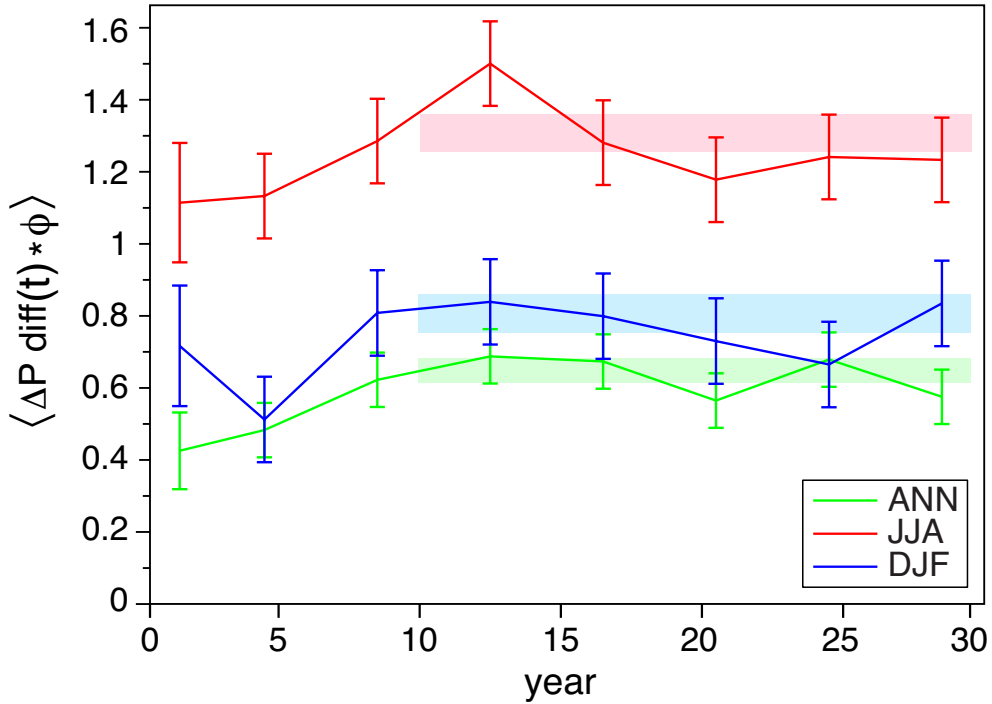
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110 *Typical precipitation change patterns for CMIP5 models.*

111 Figure S3 shows precipitation patterns corresponding to Fig. 2a of the main text,  
112 but for a selection of models from the CMIP5 archives. The selection is based on  
113 models with multiple ensemble members starting from different initial conditions  
114 for historical and RCP8.5 simulations. Multi-run ensemble means are formed  
115 over the ensemble for each model. Regional differences among these figures  
116 may be seen to be of similar order of magnitude as those investigated in the  
117 parameter perturbation runs in the main text.

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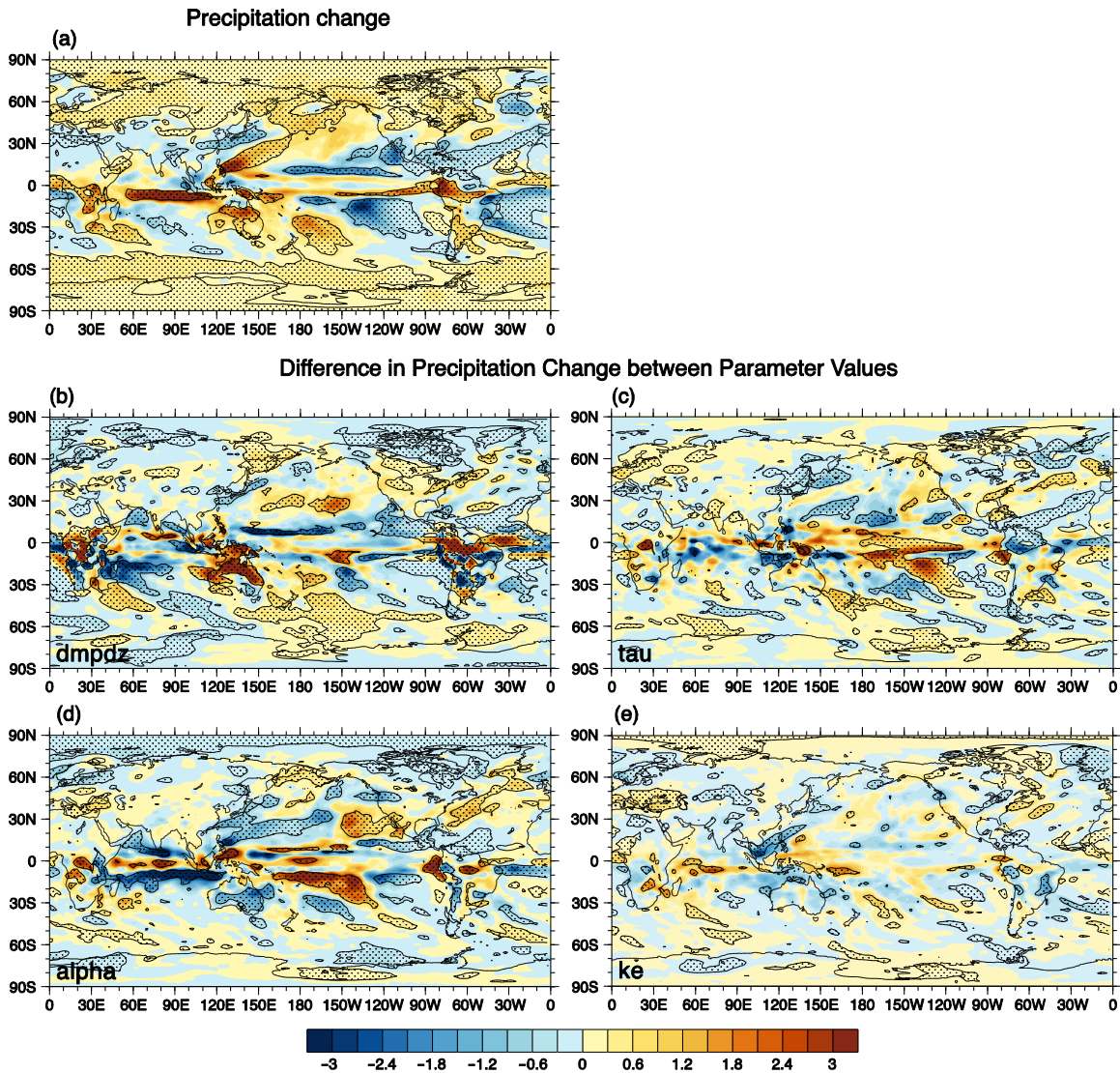
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124 **Figure S1.** Global average precipitation change across the feasible range of the  
125 entrainment parameter ( $0$  to  $2 \times 10^{-3} \text{ m}^{-1}$ ),  $\Delta P_{diff}$ , by a measure that uses a spatial  
126 projection of  $\Delta P_{diff}$  onto the pattern in Fig. 2b, showing the development of this pattern as  
127 a function of time for annual (green), June-August (red) and December-February (blue).  
128 The first point is an average over the first two years, subsequent points are four-year  
129 averages. Horizontal shaded areas show this measure of precipitation change averaged  
130 over the last 20 years, once the signal is approximately equilibrated, with the vertical  
131 extent of the shaded area indicating  $\pm 1$  standard error about the 20 year mean, as  
132 estimated from internal variability as described in the SI text.

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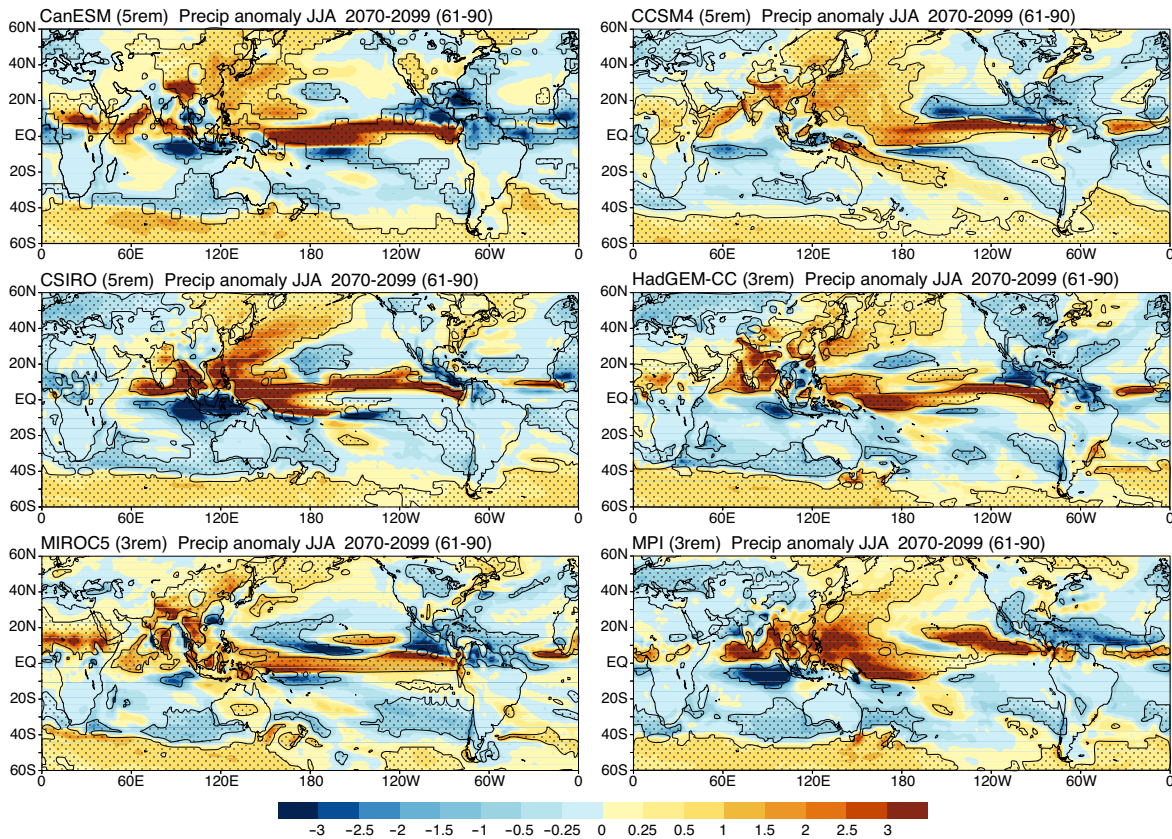


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139 **Figure S2.** (a) Precipitation (mm/day) change for 2081-2100 relative to the 1986-2005  
 140 base period under the RCP8.5 global warming scenario for CESM1 standard values for  
 141 DJF. (b)-(d) *Differences* in projected DJF precipitation change (mm/day) under global  
 142 warming (2081-2100 relative to the 1986-2005 base period) for simulations done with  
 143 different parameter values, corresponding to the JJA case shown in Fig. 2 of the main  
 144 text. Differences are across the feasible range for each parameter: (b) entrainment (case  
 145 at  $2 \times 10^{-3} \text{ m}^{-1}$  minus case at  $0 \text{ m}^{-1}$ ); (c) deep convective adjustment time (240 min case  
 146 minus 30 min case); (d) downdraft fraction (0.75 case minus case at 0); (e) evaporation  
 147 efficiency ( $1 \times 10^{-6} (\text{kg m}^{-2} \text{ s}^{-1})^{-1/2} \text{ s}^{-1}$  case minus  $0.1 \times 10^{-6} (\text{kg m}^{-2} \text{ s}^{-1})^{-1/2} \text{ s}^{-1}$  case). Stippled  
 148 areas pass a t-test at the 95% level.

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152 **Figure S3.** Examples for CMIP5 models Precipitation projections under RCP8.5  
 153 scenario for June-Aug. 2070-2099 minus historical base period 1961-1990 for: (a)  
 154 CanESM (5 members), (b) CCSM4 (5 members), (c) CSIRO (5 members), (d) HadGEM-  
 155 CC (3 members), (e) MIROC5 (3 members), (d) MPI (3 members). Stippled areas pass a  
 156 t-test at the 95% level. The number of ensemble members included in the multi-run  
 157 ensemble mean is indicated in brackets for each model.

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