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1 Interhemispheric teleconnections from tropical heat  
2 sources in intermediate and simple models

3

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PRELIMINARY ACCEPTED VERSION

## Abstract

12  
13           The mechanisms that control the interhemispheric teleconnections from tropical heat  
14 sources are investigated using an intermediate complexity model (a Quasi-Equilibrium Tropical  
15 Circulation Model, QTCM) and a simple linear two-level model with dry dynamics. Illustrating  
16 the interhemispheric teleconnection process with an Atlantic Warm Pool principal case, the heat  
17 source directly excites a baroclinic response that spreads across the equator. Three processes  
18 involving baroclinic-barotropic interactions—shear advection, surface drag, and vertical  
19 advection—then force a cross-equatorial barotropic Rossby wave response. An analysis of these  
20 processes in QTCM simulations indicates that: (1) shear advection has a pattern that roughly  
21 coincides with the baroclinic signal in the tropics and subtropics; (2) surface drag has large  
22 amplitude and spatial extent, and can be very effective in forcing barotropic motions around the  
23 globe; (3) vertical advection has a significant contribution locally and remotely where large  
24 vertical motions and vertical shear occur. The simple model is modified to perform experiments  
25 in which each of these three mechanisms may be included or omitted. By adding surface drag  
26 and vertical advection, and comparing each to shear advection, the effects of the three  
27 mechanisms on the generation and propagation of the barotropic Rossby waves are shown to be  
28 qualitatively similar to the results in QTCM. It is also found that the moist processes included in  
29 the QTCM can feed back on the teleconnection process and alter the teleconnection pattern by  
30 enlarging the prescribed tropical heating in both intensity and geographical extent, and by  
31 inducing remote precipitation anomalies by interaction with the basic state.

32

33

## 34 1. Introduction

35           Tropical heat sources can remotely influence ocean basins and continents through  
36 atmospheric teleconnections (e.g., Horel and Wallace 1981; Ropelewski and Halpert 1987;  
37 Wallace et al. 1998; Trenberth et al. 1998). In addition to many teleconnection studies in general  
38 circulation models (GCMs; e.g., Lau 1985; Mechoso et al. 1987; Kumar and Hoerling 1998;  
39 Barnston et al. 1999; Goddard and Graham 1999; Latif et al. 1999; Saravanan and Chang 2000),  
40 much has been learned from simpler models. In the tropics, heating anomalies directly force a  
41 baroclinic signal that tends to remain trapped in latitude. Thus, highly damped shallow water  
42 models (Matsuno 1966; Webster 1972; Gill 1980), which assume a vertical structure of a single  
43 deep baroclinic mode, can give a plausible first approximation to the low-level wind field in the  
44 vicinity of heating anomalies. In mid-and high-latitudes, teleconnections tend to be dominated by  
45 an equivalent barotropic signal for two reasons. Firstly, barotropic stationary or low-frequency  
46 Rossby waves in westerly flow tend to be less equatorially trapped than their baroclinic  
47 counterparts (Salby and Garcia 1987). Secondly, vertical propagation tends to reduce the  
48 contribution of baroclinic modes in the mid-latitude troposphere, leaving the signal far from the  
49 source dominated by an equivalent barotropic mode (Held et al. 1985). Thus barotropic models  
50 have been widely used to study the teleconnection response at midlatitudes (e.g., Hoskins and  
51 Karoly 1981; Simmons 1982; Simmons et al. 1983; Held and Kang 1987). However, since the  
52 heating does not directly force a barotropic response, barotropic models used to study  
53 teleconnections must prescribe a vorticity source or “Rossby wave source” (Sardeshmukh and  
54 Hoskins 1988), which can be based, for instance, on baroclinic divergence at upper levels or on  
55 baroclinic transient motions diagnosed from a GCM simulation (Held and Kang 1987). This  
56 diagnosed Rossby wave source is one convenient approach that permits the barotropic processes

57 to be examined while deferring investigation of the complex baroclinic to barotropic pathway in  
58 the tropics-to-midlatitudes teleconnection process. However, many of the terms that are  
59 specified as a fixed source in this approach are dynamical quantities whose scales, spatial form  
60 etc. depend on the interaction of the baroclinic mode with the basic state in ways that can be  
61 interesting to elucidate. Multi-level linear, steady-state wave models with both baroclinic and  
62 barotropic components comprise part of a model hierarchy (Hoskins and Karoly 1981; Ting and  
63 Held 1990; DeWeaver and Nigam 2004) that can capture at least some aspects of the tropical-  
64 baroclinic to midlatitude-barotropic transition. Interactions with baroclinic transient eddies (Held  
65 et al. 1989; Hoerling and Ting 1994) can also alter the teleconnection pattern in a manner that is  
66 not easily captured by stationary wave models.

67         The energy exchange between equatorially trapped baroclinic modes and equivalent  
68 barotropic modes with a significant projection on midlatitudes needs, therefore, to be addressed  
69 in a more sophisticated way. Instead of prescribing a Rossby wave source based on upper level  
70 divergent flow in the one level barotropic vorticity equation (e.g., Sardeshmukh and Hoskins  
71 1988, Held and Kang 1987), a series of studies have been examining this problem from the point  
72 of view of baroclinic-barotropic interaction terms and studying the effect of each mechanism at  
73 work in the baroclinic to barotropic transition. Majda and Biello (2003) develop a set of  
74 simplified asymptotic equations describing the nonlinear interaction of near-resonant long-  
75 wavelength barotropic wave trains and equatorial baroclinic wave trains in the presence of  
76 sheared zonal mean winds, and emphasize the central role of baroclinic mean shear for  
77 sufficiently rapid nonlinear exchange of energy between the tropics and midlatitudes. Biello and  
78 Majda (2004b) further examine this resonant nonlinear interaction in the presence of vertically  
79 and meridionally sheared zonal mean winds, i.e., including both meridionally symmetric and

80 antisymmetric (about the equator) vertical mean shear, and find that the effect of moderate  
81 antisymmetric winds is to shift the barotropic waves meridionally. Biello and Majda (2004a)  
82 incorporate the dissipative mechanisms arising from radiative cooling and atmospheric boundary  
83 layer drag, to explain how this mechanism creates barotropic/baroclinic spin up/spin down in the  
84 teleconnection process. Their results indicate that although the dissipation slightly weakens the  
85 tropics to midlatitude connection, strong localized wave packets are nonetheless able to  
86 exchange energy between barotropic and baroclinic waves on intraseasonal timescales in the  
87 presence of baroclinic mean shear. Wang et al. (2010) examine how, in the presence of  
88 background vertical shear, the transition from equatorial baroclinic mode to equivalent  
89 barotropic mode at midlatitudes establishes the interhemispheric influence of the Atlantic Warm  
90 Pool (AWP) in the northern hemisphere on the south eastern Pacific.

91         In this work, we aim at directly diagnosing and assessing the relative importance of the  
92 interaction terms between the baroclinic and barotropic modes that appear as source terms in the  
93 barotropic equation. These interaction terms are similar to a Rossby-wave source approach in  
94 that these terms appear as a vorticity source in the barotropic equation, but the “source” can be  
95 quantitatively and conceptually quite different than approaches based on upper level divergent  
96 flow in a single-level vorticity equation. For instance, if there is no vertical shear and no  
97 damping on the baroclinic mode associated with surface stress, then upper level divergence in  
98 the baroclinic mode does not produce any linear forcing of the barotropic mode. At the same  
99 time, by explicitly modeling the gravest baroclinic mode, the teleconnection pathway can be  
100 followed as the two modes interact, for instance with the baroclinic mode producing a  
101 teleconnection across the equator, and then interactions yielding a barotropic mode that can  
102 propagate to higher latitudes in the opposite hemisphere. Building on previous work with

103 idealized asymptotic equations, here we use realistic background states and more detailed  
104 physics including moist processes to analyze teleconnections arising from tropical heat sources.

105         We use two numerical models with different complexity, in both of which the baroclinic-  
106 barotropic interactions are explicitly formulated. The more complex one is a Quasi-Equilibrium  
107 Tropical Circulation Model (QTCM) (Neelin and Zeng 2000), in which part of the quasi-  
108 equilibrium convective closure is used to carry forward analytically the model solution for the  
109 baroclinic vertical structure in the convective regions. The full primitive equations are then  
110 projected on the resulting baroclinic plus barotropic basis functions for vertical structure. This  
111 intermediate complexity model retains some of the simplicity of the analytical solutions, while  
112 keeping full nonlinearity from the primitive equations, and a consistent representation of moist  
113 processes including a deep convective parameterization. The consistent vertical mode  
114 decomposition yields three mechanisms (Neelin and Zeng 2000) for excitation terms in the  
115 barotropic equations due to baroclinic terms: interactions of vertical shear in horizontal advection  
116 terms, vertical advection of vertically sheared motions, and interactions via surface stress in the  
117 boundary layer. The QTCM thus allows for quantifying the effect of each of those mechanisms,  
118 and to assess the role of feedbacks associated with moist processes. The simpler model we use is  
119 based on that of Lee et al. 2009), which is a two-level steady-state wave model linearized about  
120 background flows. In preparation for the present study, the Lee et al. (2009) version was  
121 extended to include the three mechanisms for excitation of barotropic modes present in the  
122 QTCM. The simple model permits experiments in which mechanisms may be included or  
123 omitted. Therefore, an assessment of individual impacts is obtained by retaining the forcing  
124 terms one at a time in the barotropic equation, and inspecting the differences in the  
125 teleconnection patterns obtained with each mechanism. Our primary focus is on the heat source

126 region above the Atlantic Warm Pool (AWP) because previous studies have shown that it has  
127 significant interhemispheric influences (e.g., Wang et al. 2010).

128 The remainder of the text is organized as follows. Section 2 gives a brief introduction of  
129 the two models as well as the modifications made for the study. Section 3 presents the QTCM  
130 experiments, examines each of the three forcing terms of barotropic Rossby waves, and explores  
131 the effect of moist feedback in the teleconnection process. Section 4 presents the simple model  
132 experiments, narrowing down on the role of each forcing term. Section 5 consists of a summary  
133 and discussion.

134

## 135 2. Models and Methodology

### 136 *a. QTCM*

137 The QTCM belongs in a class of tropical atmospheric model of intermediate complexity  
138 that occupies a niche between GCMs and simple models. In the QTCM, the derivation from the  
139 primitive equations is done systematically and the constraints placed on the baroclinic flow by  
140 the GCM convective parameterizations with quasi-equilibrium (QE) thermodynamic closures are  
141 exploited. Part of the QE convective closure can be used to carry forward analytically the model  
142 solution for the vertical structure in convective regions. Using the vertical structures based on  
143 these analytical solutions as the leading basis functions in a Galerkin projection of the primitive  
144 equations, self-consistent nonlinear terms can be retained in advection, moist convection, and  
145 vertical momentum transfer terms, among others. A more detailed model description can be  
146 found in Neelin and Zeng (2000). The model performance has been analyzed in Zeng et al.  
147 (2000) for climatology, and in Lin et al. (2000) and Lin and Neelin (2000, 2002) for



148 intraseasonal variability. Moist teleconnection mechanisms within the tropics have been  
 149 examined using this model in Su and Neelin (2002) and Neelin and Su (2005).

150 The present study uses the QTCM1 version 2.3 which retains a single basis function for  
 151 the vertical structure of temperature. This is the simplest configuration, but with considerable  
 152 success in capturing tropical phenomena, since the temperature structure matches the  
 153 consequences of a quasi-equilibrium convective scheme, and the baroclinic velocity basis  
 154 function is analytically compatible. This provides an appealing system for baroclinic-barotropic  
 155 decomposition. One might anticipate that an additional degree of freedom in the boundary layer  
 156 might alter some surface drag effects quantitatively. The numerical implementation of the  
 157 QTCM1 here covers the domain from 78.75°S to 78.75°N and over all longitudes, with a  
 158 horizontal resolution of 3.75° latitude and 5.625° longitude.

159 A brief review of the equation for the barotropic wind component in the QTCM is  
 160 presented below to aid the analysis of the barotropic teleconnection process in the following  
 161 sections. A summary of the QTCM1 equations are given for reference in Appendix. Using  $V_0$  and  
 162  $V_1$  as the basis functions for velocity, the projected barotropic vorticity equation in Neelin and  
 163 Zeng (2000) is:

$$164 \quad \partial_t \zeta_0 + \text{curl}_z(\mathcal{D}_{V_0}(\mathbf{v}_0, \mathbf{v}_1)) + \beta v_0 = -\text{curl}_z(\varepsilon_0 \mathbf{v}_0) - \text{curl}_z(\varepsilon_{10} \mathbf{v}_1) \quad (1)$$

165 where subscripts 0 and 1 denote barotropic and baroclinic component, respectively, and  
 166  $\mathcal{D}_{V_0}(\mathbf{v}_0, \mathbf{v}_1)$ , the operator containing nonlinear advection terms and horizontal diffusion is given  
 167 by:

$$168 \quad \mathcal{D}_{V_0}(\mathbf{v}_0, \mathbf{v}_1) = \mathbf{v}_0 \cdot \nabla \mathbf{v}_0 + \langle V_1^2 \rangle \mathbf{v}_1 \cdot \nabla \mathbf{v}_1 + \langle V_1^2 \rangle (\nabla \cdot \mathbf{v}_1) \mathbf{v}_1 - K_H \nabla^2 \mathbf{v}_0 \quad (2)$$

169 where the term in brackets denote vertical averages over the troposphere  $\langle X \rangle = p_T^{-1} \int_{p_n}^{p_s} X dp$ . For

170 the analysis of Rossby wave sources in the QTCM, we rearrange (1) to obtain:

$$\begin{aligned}
 & \partial_t \nabla^2 \psi_0' + \text{curl}_z(\mathbf{v}_0 \cdot \nabla \mathbf{v}_0)' - K_H \nabla^4 \psi_0' + \beta v_0' \\
 171 \quad & = -\text{curl}_z(\langle V_1^2 \rangle \mathbf{v}_1 \cdot \nabla \mathbf{v}_1)' - \text{curl}_z(\langle V_1^2 \rangle (\nabla \cdot \mathbf{v}_1) \mathbf{v}_1)' - \text{curl}_z(\varepsilon_0 \mathbf{v}_0 + \varepsilon_{10} \mathbf{v}_1)' \quad (3)
 \end{aligned}$$

172 where  $\psi_0$  is the barotropic stream function, and (') denotes anomalies defined as the difference

173 between a climatological run and a run with an imposed heating anomaly. The stationary

174 barotropic Rossby wave response (i.e. of the l.h.s. of (3)) to a localized source is well known

175 (e.g., Hoskins and Karoly 1981, Simmons et al. 1983; Held and Kang 1987) so we focus on the

176 comparison of the forcing terms on the r.h.s. of (3). The three forcing sources of the barotropic

177 motion that involve the interactions with baroclinic motion are defined as follows: 1) the shear

178 advection term  $-\text{curl}_z(\langle V_1^2 \rangle \mathbf{v}_1 \cdot \nabla \mathbf{v}_1)'$ , which represents advective interactions of the baroclinic

179 wind component (with vertical shear); 2) the vertical advection term  $-\text{curl}_z(\langle V_1^2 \rangle (\nabla \cdot \mathbf{v}_1) \mathbf{v}_1)'$ ,

180 which represents the effect of vertical motion advecting the baroclinic wind component; 3) the

181 surface drag term  $-\text{curl}_z(\varepsilon_0 \mathbf{v}_0 + \varepsilon_{10} \mathbf{v}_1)'$ , which derives from surface stress  $-(g / p_T) \tau_s$  (with

182 zero stress at model top) and a bulk formula parameterization  $\tau_s = \tau|_{p_s} = \rho_a C_D V_s \mathbf{v}_s$ . These three

183 forcing mechanisms of the barotropic motion involved in the baroclinic-barotropic interactions

184 are further discussed in section 3b in the teleconnection experiments. We further note that

185 linearizing the interaction terms in (3) yields:

$$186 \quad -\text{curl}_z(\langle V_1^2 \rangle \bar{\mathbf{v}}_1 \cdot \nabla \mathbf{v}_1' + \langle V_1^2 \rangle \mathbf{v}_1' \cdot \nabla \bar{\mathbf{v}}_1) - \text{curl}_z(\langle V_1^2 \rangle (\nabla \cdot \mathbf{v}_1') \bar{\mathbf{v}}_1 + \langle V_1^2 \rangle (\nabla \cdot \bar{\mathbf{v}}_1) \mathbf{v}_1') - \text{curl}_z(\varepsilon_0 \mathbf{v}_0' + \varepsilon_{10} \mathbf{v}_1').$$

187 The linearized interaction terms make it clear that if there is no vertical shear or vertical velocity

188 in the mean state ( $\bar{\mathbf{v}}_1 = 0$ ) and no drag on the baroclinic mode ( $\varepsilon_{10} = 0$ ), then the baroclinic mode  
189 can have any vertical velocity ( $\nabla \cdot \mathbf{v}'_1$ ), but there will be no forcing of the barotropic mode. This  
190 appears quite different from the assumptions used in traditional Rossby wave source approaches  
191 based on a vorticity equation at upper levels, but is similar in the sense that it diagnoses a  
192 vorticity source that drives the barotropic equation, in this case the equation for the full  
193 barotropic mode. We will refer to this as a "barotropic Rossby wave source" for clarity since it is  
194 the vorticity source term as it occurs projected on the full barotropic mode. We also note that  
195 while we have retained the whole surface stress term on the right-hand side above, arguably it is  
196 more consistent to move the barotropic component of this, i.e.,  $-\text{curl}_z(\varepsilon_0 \mathbf{v}'_0)$ , to the l.h.s. in (3)  
197 since it acts as a drag on the barotropic mode. In that case the surface drag contribution to the  
198 barotropic Rossby wave source due to the baroclinic mode is simply  $-\text{curl}_z(\varepsilon_{10} \mathbf{v}'_1)$ . We will show  
199 examples of both in diagnostics.

200

### 201 *b. Simple model*

202 The simple model we use in this study is based on that developed by Lee et al. (2009).  
203 This is a two-level model, in which equations are recast as baroclinic and barotropic components,  
204 and are linearized about prescribed background wind fields. The model is designed to simulate  
205 both the local and remote stationary response of the atmosphere when forced with a localized  
206 heating. In this model, the baroclinic response to tropical heating anomalies is essentially the  
207 same as described by the Matsuno-Gill model (Matsuno 1966; Gill 1980) with damping used in  
208 Lee et al (2009). This baroclinic response then excites a barotropic response by advective

209 interactions with vertical background wind shear (i.e., through the shear advection mechanism),  
 210 and the barotropic signals are in turn transmitted to high latitudes.

211 Our modification of the Lee et al. (2009) model allows for consideration of surface drag  
 212 as another mechanism of baroclinic-barotropic interactions. This was done by eliminating, from  
 213 the relative vorticity equations, the linear momentum damping  $-r\nabla^2\psi$  both in the upper  
 214 (250mb) and lower (750mb) levels, and adding in the lower level a term  $-r_s\nabla^2\psi$ , where the  
 215 surface drag coefficient is  $r_s = (g / p_T)\rho_a C_D V_s$ . Thus, in the barotropic and baroclinic vorticity  
 216 equations, the linear damping coefficients  $r_0$  and  $r_1$  become  $r_0 = r_1 = r_s / 2$ . We set  $r_s = (3.5\text{day})^{-1}$   
 217 for  $p_T = 500\text{mb}$ ,  $C_D = 10^{-3}$ ,  $V_s = 10\text{m s}^{-1}$ . The simple model (as modified relative to Lee et al  
 218 2009) is thus given by the following barotropic and baroclinic vorticity equations:

$$219 \quad \frac{1}{a \cos \theta} \left[ \frac{\partial}{\partial \lambda} (\bar{u}_0 \nabla^2 \psi'_0 + u'_0 \nabla^2 \bar{\psi}_0) + \frac{\partial}{\partial \theta} (\cos \theta \bar{v}_0 \nabla^2 \psi'_0 + \cos \theta v'_0 \nabla^2 \bar{\psi}_0) \right] + 2\Omega \frac{v'_0}{a} \quad (4)$$

$$= -r_0 \nabla^2 \psi'_0 + r_0 \nabla^2 \psi'_1 + A_0 \nabla^4 \psi'_0 + F_{\psi_0}$$

$$220 \quad \frac{1}{a \cos \theta} \left[ \frac{\partial}{\partial \lambda} (\bar{u}_1 \nabla^2 \psi'_1 + u'_1 \nabla^2 \bar{\psi}_1) + \frac{\partial}{\partial \theta} (\cos \theta \bar{v}_1 \nabla^2 \psi'_1 + \cos \theta v'_1 \nabla^2 \bar{\psi}_1) \right] + 2\Omega \frac{v'_1}{a} \quad (5)$$

$$= -r_1 \nabla^2 \psi'_1 + r_1 \nabla^2 \psi'_0 + A_1 \nabla^4 \psi'_1 + F_{\psi_1}$$

221 where subscripts 0 and 1 denote barotropic and baroclinic mode respectively, variables are  
 222 separated into the basic state and anomaly components denoted by bar and prime terms,  $A_0$  and  
 223  $A_1$  are the momentum diffusion coefficient for barotropic and baroclinic motion respectively. The  
 224 differences from the model in Lee et al. (2009) are the two terms  $r_0 \nabla^2 \psi'_1$  and  $r_1 \nabla^2 \psi'_0$  that derive  
 225 from the surface drag mechanism. The  $F_{\psi}$  terms represent the vorticity tendency terms due to the

226 shear advection and vertical advection mechanisms of baroclinic-barotropic interactions. The  
 227 complete form of  $F_{\psi_0}$  is:

$$\begin{aligned}
 F_{\psi_0} &= \frac{1}{a \cos \theta} \left[ \frac{\partial}{\partial \lambda} (\bar{u}_1 \nabla^2 \psi_1' + u_1' \nabla^2 \bar{\psi}_1) + \frac{\partial}{\partial \theta} (\cos \theta \bar{v}_1 \nabla^2 \psi_1' + \cos \theta v_1' \nabla^2 \bar{\psi}_1) \right] \\
 228 \quad &= \frac{1}{a \cos \theta} \left\{ \nabla^2 \psi_1' \left[ \frac{\partial \bar{u}_1}{\partial \lambda} + \frac{\partial}{\partial \theta} (\cos \theta \bar{v}_1) \right] + \nabla^2 \bar{\psi}_1 \left[ \frac{\partial u_1'}{\partial \lambda} + \frac{\partial}{\partial \theta} (\cos \theta v_1') \right] \right. \\
 &\quad \left. + \left[ \bar{u}_1 \frac{\partial \nabla^2 \psi_1'}{\partial \lambda} + \bar{v}_1 \frac{\partial}{\partial \theta} (\cos \theta \nabla^2 \psi_1') \right] + \left[ u_1' \frac{\partial \nabla^2 \bar{\psi}_1}{\partial \lambda} + v_1' \frac{\partial}{\partial \theta} (\cos \theta \nabla^2 \bar{\psi}_1) \right] \right\} \quad (6)
 \end{aligned}$$

229 The first term in the r.h.s. of (6) represents the vertical advection of anomalous baroclinic  
 230 vorticity via background vertical wind. The second term represents the vertical advection of  
 231 background baroclinic vorticity via anomalous vertical wind. The third term represents the zonal  
 232 and meridional advection of anomalous baroclinic vorticity via background zonal and meridional  
 233 shear. The fourth term represents the zonal and meridional advection of background baroclinic  
 234 vorticity via anomalous zonal and meridional shear.

235 The thermodynamic equation is given by:

$$236 \quad \gamma \phi_1 + c_g^2 \nabla^2 \chi_1 = -Q \quad (7)$$

237 where  $\gamma$  is the thermal damping coefficient,  $\phi_1$  is the baroclinic geopotential,  $c_g$  is the internal  
 238 gravity wave speed,  $\chi_1$  is the baroclinic divergence and  $Q$  is the diabatic heating rate. Note that  
 239 the simple model is explicitly steady state and linear and omits all moisture effects. The  
 240 equations (4)-(7) together with a baroclinic divergence equation (not shown here) are in a closed  
 241 form and are the governing equations solved in the simple model.

242 In our simple model experiments, we are able to activate and deactivate each forcing  
 243 mechanism—the surface drag, the vertical advection and the shear advection, and compare the  
 244 effects of each forcing with those in the QTCM results.

245 The numerical implementation of the three versions of the simple model covers the  
 246 domain from 90°S to 90°N over all longitudes, with a horizontal resolution of 4.5° latitude and  
 247 4.5° longitude.

248

249 *c. Methodology*

250 We concentrate on the period of June-August (JJA), during which the tropical heating  
 251 and precipitation anomalies develop to their maximum strength in the northern hemisphere  
 252 summer, including in the AWP region of interest here. In JJA, the subtropical jets are strong in  
 253 the southern (winter) hemisphere, which can favor the shear advection mechanism for  
 254 interhemispheric teleconnections (Wang et al. 2010). Accordingly, in both the QTCM and simple  
 255 model, the zonal mean of the barotropic and baroclinic wind fields are prescribed as the JJA  
 256 zonal means. The time advance of the zonal mean fields in the QTCM is, therefore, bypassed.  
 257 The prescribed velocities correspond to the streamfunction at the 250 and 750mb levels from the  
 258 monthly NCEP-NCAR reanalysis (Kalnay et al. 1996):

259 
$$\bar{u}_0 = -\frac{\partial}{\partial y} \bar{\psi}_0^{ncep} = -\frac{\partial}{\partial y} [(\bar{\psi}_{250}^{ncep} + \bar{\psi}_{750}^{ncep}) / 2] \quad (8)$$

260 
$$\bar{u}_1 = -\frac{\partial}{\partial y} \bar{\psi}_1^{ncep} = -\frac{\partial}{\partial y} [(\bar{\psi}_{250}^{ncep} - \bar{\psi}_{750}^{ncep}) / 2] \quad (9)$$

261 Further, in the QTCM we replace the zonal velocity that advects the temperature gradient  
262 by that corresponding to the zonal mean basic state velocity as in equations (8) and (9). This  
263 procedure removes the main source term for baroclinic instability, thus reducing weather  
264 variability. There are some trade-offs here. On the one hand, due to reduction in poleward fluxes,  
265 more moisture is available for precipitation in the subtropics, and interactions of the  
266 teleconnections with storm tracks are suppressed. On the other hand, the procedure has several  
267 advantages in view of our goals. These include (i) statistically significant signals are easy to  
268 detect in decadal runs, (ii) comparison to the simple model is facilitated, (iii) the basic state on  
269 which wave propagation occurs is strongly constrained towards observations, and (iv)  
270 interpretation in terms of stationary wave propagation is more straightforward. This should thus  
271 be viewed as an intermediate step between simple models and GCMS that would potentially  
272 include more complex effects such as interaction with baroclinic transients.

273

### 274 3. QTCM Experiments and Results

#### 275 *a. Atlantic Warm Pool (AWP) teleconnection experiments set up*

276 In this experiment, we prescribe a Gaussian-shaped baroclinic heating anomaly as in Lee  
277 et al. (2009). The anomaly amplitude is  $169.2\text{W/m}^2$  (which is equivalent to 6mm/day of  
278 precipitation) at the center at (20°N, 70°W), and the zonal and meridional length scales are 5°  
279 latitude and 15° longitude (see Fig. 1a). The model is then run for ten years using monthly  
280 climatological SSTs (Reynolds and Smith 1994).

281 Figure 1b shows the precipitation response averaged over the June-August for ten years  
282 in response to the prescribed heating anomalies in this experiment. It can be seen that the latent

283 heat associated with the precipitation anomalies enhance the local prescribed heating anomalies  
284 to a significant extent, and thus will enhance the teleconnection response in comparison to a  
285 model with dry dynamics. The shape of the heating is also slightly modified from the prescribed.  
286 We return to this moist feedback effect in section 3c.

287

288 *b. AWP teleconnections analysis*

289 The JJA mean baroclinic and barotropic streamfunctions anomalies are shown in Figs. 2a  
290 and 2b. The baroclinic mode resembles the Gill–Matsuno-type response (Matsuno 1966; Gill  
291 1980) and is equatorially trapped with most of the signal within equatorial deformation radius.  
292 An important aspect is that the off-equatorial heating projects sufficiently on the Kelvin mode (to  
293 the east of the heating) and the symmetric Rossby modes (to the west) that a substantial  
294 baroclinic signal crosses the equator. The barotropic mode shows an interesting pattern.  
295 Typically, a pure barotropic stationary Rossby wave propagating in a westerly region of the mid-  
296 latitudes in an approximately barotropic basic state will approach a critical latitude where  $\bar{u} = 0$   
297 and thus will not propagate directly across the region of easterlies near equator. In our  
298 experiments, however, the barotropic signal has a significant component in the southern  
299 hemisphere. This is because the QTCM includes a full set of forcing sources of the barotropic  
300 motions through baroclinic-barotropic interactions. As mentioned in section 2a, in the model’s  
301 barotropic component equation in QTCM, the three baroclinic forcing mechanisms—the shear  
302 advection, surface drag, and vertical advection— actively generate barotropic wave trains in the  
303 equatorial regions and within the southern hemisphere westerlies.

304 To explore the relative importance of the three mechanisms of interest in the QTCM  
305 AWP experiment, we plot in Figs. 3a, 3b, 3c the amplitudes of the three terms in the r.h.s. of (3),



306 and in Figs. 4a, 4b, 4c their inverse Laplacians, i.e., the equivalent barotropic streamfunction  
 307 tendency terms. Shaded areas in Figs 3 and 4 represent values that are statistically significant  
 308 with a confidence level of 99% from a student's t-test. The shear advection term  
 309  $-curl_z(\langle V_1^2 \rangle \mathbf{v}_1 \cdot \nabla \mathbf{v}_1)'$  shows a large dipole in the tropics (Fig. 3a and 4a), roughly coincident  
 310 with where the baroclinic signal is strong. The southwest to northeast angle reflects the  
 311 corresponding tilt seen in Fig. 2 close to the zero contour of  $\psi_1$  where the strong gradient in  $\psi_1$   
 312 indicates strong baroclinic wind anomalies. Thus the region of strong shear forcing reflects the  
 313 heating-forced baroclinic anomalies which, while equatorially trapped, are able to propagate into  
 314 the southern hemisphere where they can excite barotropic waves.

315 The magnitude of the surface drag term  $-curl_z(\varepsilon_0 \mathbf{v}_0 + \varepsilon_{10} \mathbf{v}_1)'$  in Fig. 3b is not locally as  
 316 large as that of the shear advection term (Fig. 3a) and vertical advection term (Fig. 3c), but its  
 317 inverse Laplacian (Fig. 4b) shows large values around the heat source with amplitudes  
 318 comparable with the vertical advection term. The geographical spread of the surface drag forcing  
 319 is broader in both hemispheres than the two other mechanisms. Note that Figs. 3b and 4b show  
 320 the net effect of surface drag mechanism, i.e., the amplitude of the baroclinic forcing  
 321  $-curl_z(\varepsilon_{10} \mathbf{v}_1)'$  after compensation by linear damping  $-curl_z(\varepsilon_0 \mathbf{v}_0)'$ . Also note that the sign of the  
 322 coefficient of transfer by surface stress between baroclinic and barotropic wind components  $\varepsilon_{10}$  is  
 323 negative in order that all the turbulence terms have the same form (refer to the appendix for more  
 324 detail). For a rough estimate of this compensation, comparing the amplitudes of  $-\varepsilon_{10} \psi_1$  (where  
 325  $\varepsilon_{10} = (-28 \text{day})^{-1}$  and  $\psi_1$  can be approximated from the values in Fig. 2a) and  $-\varepsilon_0 \psi_0$  (where  
 326  $\varepsilon_0 = (5.6 \text{day})^{-1}$  and  $\psi_0$  can be approximated from the values in Fig. 2b), indicates that the  
 327 compensation effect of the linear damping can be as large as 50% of the baroclinic forcing. This

328 estimate is confirmed by Fig. 3d, showing only the baroclinic forcing component of the surface  
 329 drag  $-curl_z(\varepsilon_{10}\mathbf{v}'_1)$ . As expected, this component is roughly twice as large locally as the total  
 330 surface drag term (Fig. 3b). We can also see that the surface drag component has a significant  
 331 contribution in the southern hemisphere. Thus the baroclinic forcing from the surface drag term  
 332 can potentially exert a substantial impact on the generation and propagation of barotropic Rossby  
 333 waves, especially in the southern hemisphere corresponding to the  $\psi_1$  response there.

334 Finally, the vertical advection term  $-curl_z(\langle V_1^2 \rangle (\nabla \cdot \mathbf{v}_1)\mathbf{v}_1)'$  (Figs. 3c and 4c) shows a  
 335 localized forcing around the heat source where the vertical velocity is large (also see Fig. 1b for  
 336 large local precipitation anomaly there). Note that some degree of compensation can occur with  
 337 the surface drag term in regions of upward vertical motion where the vertical velocity term  
 338 contribution  $-\langle V_1^2 \rangle (\nabla \cdot \bar{\mathbf{v}}_1)curl_z\mathbf{v}'_1$  has opposite sign but similar form to  $-curl_z(\varepsilon_{10}\mathbf{v}'_1)$ . Far from the  
 339 heat source, in certain regions of the Pacific and Indian Ocean, the vertical velocity term can still  
 340 have fairly substantial contributions corresponding to the remote precipitation anomalies in those  
 341 regions. The strong vertical advection forcing locally around the heat source (Fig. 3c) and the  
 342 remote signals in the southern hemisphere imply that this mechanism has a substantial role in the  
 343 interhemispheric teleconnections, and should not be neglected.

344

### 345 *c. Moist feedback*

346 The precipitation response in the QTCM AWP experiments is shown in Fig. 1b. There is  
 347 clear evidence that moist processes enhance the teleconnection process. First, moist feedback  
 348 enhances the prescribed anomalous heat source locally by approximately 6mm/day in this  
 349 experiment, which is as large as the prescribed heat source. Second, the shape of the precipitation  
 350 anomaly is stretched southwestward into eastern Pacific region. A similar feature is apparent in

351 the GCM AWP experiments in Wang et al. (2007, 2008). This precipitation anomaly is the result  
352 of the Atlantic Warm Pool-induced subtropical Rossby waves propagating westward and  
353 interacting with the Intertropical Convergence Zone (ITCZ) in the eastern Pacific. The impact of  
354 this convective heating anomaly in the eastern Pacific is further analyzed in section 3d. Third,  
355 this elongated shape, and the compensating subsidence north of the precipitation anomaly are  
356 consistent with the mechanism described in Chou and Neelin (2003) as the result of the  
357 interaction between baroclinic Rossby wave dynamics and convective heating. The subsidence  
358 may modestly impact the teleconnection patterns north of the heating anomaly by reducing the  
359 baroclinic signal extent and by contributing to vertical advection. Finally, as the flow anomalies  
360 produced by the teleconnections interact with moist processes remotely, e.g., advecting the basic  
361 state moisture gradient, they can induce remote precipitation anomalies that can contribute to the  
362 baroclinic-barotropic interaction. For instance, Fig. 1b shows precipitation anomalies in the  
363 equatorial Western Pacific and in the subtropical Southeastern Pacific. The latter corresponds to  
364 a significant contribution to the vertical advection forcing term in Figs. 3c and 4c in the southern  
365 hemisphere.

366

367 *d. The impact of the response in the eastern Pacific ITCZ region*

368 As mentioned in section 3c, the moist feedback on the teleconnections leads to an  
369 elongation of the anomalous heat source in the AWP region into the eastern Pacific ITCZ region.  
370 This elongation is also seen in the AGCM experiments of Wang et al. (2007, 2008). Here, we  
371 investigate quantitatively the influence of this additional heating in the ITCZ region on the AWP  
372 teleconnections into the southern hemisphere. We prescribe a similar Gaussian-shaped baroclinic  
373 heating anomaly with the same amplitude as in the one above the AWP, but with the center at

374 (15°N, 95°W), and scales of 3.0° latitude and 7.5° longitude. The model is then run for ten years  
375 using monthly climatological SSTs (Reynolds and Smith 1994).

376 Fig. 5 shows the barotropic streamfunction response to the heating prescribed in the  
377 eastern Pacific region. A comparison between this and Fig. 2b, reveals an overlap of the positive  
378 and negative phases of the response induced by the two different heating regions, and confirms  
379 that the induced eastern Pacific heating provides a positive feedback to the original AWP  
380 heating. We have also tested the result's sensitivity to the extension of the elongation, and found  
381 that the model response to a further elongation into the eastern Pacific as that in the AGCM  
382 experiments of Want et al. (2007, 2008) has an extremely similar pattern (not shown).

383

384 e. *Sensitivity of the teleconnection pattern to longitudinal location of heating anomaly*

385 To explore the dependence of the teleconnection response to the heating location in  
386 longitude, we perform a supplementary experiment in which the heating source is placed in the  
387 central Pacific at a location 90° in longitude west of the AWP (see Fig. 6a). The precipitation  
388 anomalies in this experiment are shown in Fig. 6b, while the baroclinic and barotropic  
389 streamfunctions response are shown in Figs. 7a and 7b, respectively. The zonally asymmetric  
390 basic state in the model can affect wave propagation, but some of the most obvious differences  
391 arise in the moist response to the source. The precipitation anomalies do not show a similar  
392 elongation as those in the AWP experiment (Fig. 1b), which leads to smaller zonal wavelengths  
393 in the baroclinic and hence in the barotropic response (Fig. 7b). Based on the WKB theory for  
394 stationary barotropic Rossby wave propagation in latitudinally varying flow, the local meridional  
395 wave number  $l(y)$  is given by  $l(y) = \pm(\hat{\beta}\bar{u}_m^{-1} - k^2)^{1/2}$ , where  $k$  is the zonal wave number,  $\hat{\beta}$   
396 and  $\bar{u}_m$  are basic state vorticity and zonal mean flow variables defined in Mercator coordinates

397 equivalent to the form on a beta-plane with spherical effects incorporated (Hoskins and Karoly  
398 1981). The smaller zonal wavelengths (larger zonal wave number  $k$ ) mean a lower turning  
399 latitude because the local meridional wave number for stationary barotropic Rossby waves goes  
400 to zero at smaller values of  $\hat{\beta}\bar{u}_m^{-1}$ . Thus the wave arc in the northern hemisphere is more zonal.  
401 In the southern hemisphere, the barotropic responses in both the AWP and central Pacific  
402 experiments (Figs. 2b and 7b) are qualitatively similar, but the latter one has weaker magnitudes.  
403 This is partly due to the small baroclinic response in the southern hemisphere (Fig. 7a), and to  
404 the absence of the vertical advection forcing sources in the southern Pacific (Figs. 3c and 4c).

405

## 406 4. Simple Model experiments

407 In the simple model, an identical Gaussian-shaped heating anomaly is prescribed in the  
408 AWP region with a diabatic heating rate of  $2.5 \times 10^{-2} \text{ W kg}^{-1}$ , which is equivalent to  
409  $2.15 \text{ K day}^{-1}$  at 500mb. For the simple vertical structure of this model (linear within each layer),  
410 this would be roughly equivalent to  $127.6 \text{ W m}^{-2}$  using 500mb layer depth. This heating  
411 anomaly is the only heat source since there is no moist feedback in the model. Recall from  
412 section 2, that the model is linearized about the basic state from JJA NCEP-NCAR reanalysis  
413 streamfunction averaged zonally around the globe. Other model parameters used in the present  
414 study are the same as those in Lee et al. (2009) with the following exceptions. The barotropic  
415 and baroclinic linear damping coefficient is set to  $(3.5 \text{ day})^{-1}$  for compatibility with the QTCM;  
416 and the barotropic horizontal mixing coefficient is set to  $2.5 \times 10^5 \text{ m}^2 \text{ s}^{-1}$  following Wang et al  
417 (2010). Altering these damping coefficients affects the rate at which the barotropic wave decays.

418           Figures 8a shows the barotropic streamfunctions response in the model with shear  
419 advection mechanism, and Fig. 8b shows the corresponding values with both shear advection and  
420 surface drag mechanisms included (Note that the latitude coverage is adjusted to 78.75°S to  
421 78.75°N in order to compare with the QTCM results). Addition of the surface drag mechanism  
422 results in a strong amplification and extension of the barotropic response in the southern  
423 hemisphere. This supports the finding in the QTCM experiments that the surface drag  
424 mechanism is potentially very effective in forcing the barotropic response globally, especially in  
425 spreading the cross-equatorial barotropic signals.

426           Figure 8c shows the barotropic streamfunction response of the model experiment with  
427 both the shear advection and the vertical advection mechanisms. Comparing with Fig. 8a, as in  
428 the QTCM experiment, the vertical advection amplifies the barotropic response locally around  
429 the heating area, and spreads the barotropic signals into the southern hemisphere, although the  
430 impact is moderate compared to the surface drag mechanism.

431

## 432 5. Summary and discussion

433           We have investigated the mechanisms that control the interhemispheric  
434 teleconnections from tropical heat sources. Our approach is based on the analysis of the response  
435 to idealized distributions of tropical heating sources in experiments in QTCM and in a simple  
436 steady-state, damped, linear stationary wave model. We concentrated primarily in the Atlantic  
437 Warm Pool region to prescribe the heating because it has been identified as significant in setting  
438 up interhemispheric influence in previous studies (e.g., Wang et al. 2010). The direct baroclinic  
439 response to this tropical heating is approximately a Gill–Matsuno-type response (Matsuno 1966;

440 Gill 1980), which is equatorially trapped. The teleconnections to mid and high latitudes are  
441 dominated by barotropic mode. The baroclinic to barotropic pathway is complex involving the  
442 basic state shear with all its spatial dependence, as well as the basic state vertical velocity and  
443 surface drag. In absence of basic state shear and vertical velocity and of surface drag, baroclinic  
444 and barotropic components are decoupled. This makes the recent literature examining the role of  
445 these interaction terms as a driver for barotropic motions from heat forced baroclinic motions  
446 (e.g., Neelin and Zeng 2000, Majda and Biello 2003, Lee et al. 2009) appear very different from  
447 the earlier literature that assumed upper-level divergence and related terms could be viewed as a  
448 driver (e.g., Sardeshmukh and Hoskins 1988, Held and Kang 1987), often summarized as a  
449 vorticity source term (the "Rossby wave source") for a single-level barotropic equation. Here we  
450 diagnose the interaction terms as a consistent vorticity source for the barotropic mode in a  
451 primitive equation model that has an explicit vertical mode decomposition. In addition to explicit  
452 computation of the interaction terms as in earlier theoretical studies, the study retains a complex  
453 three-dimensional basic state and moist processes for a quantitative examination.

454         The interaction-term framework results in some very substantial differences in the way  
455 one views the teleconnections generated by anomalous heating. First, it should be noted that  
456 upper-level divergence in the baroclinic mode does not necessarily drive a response in the  
457 barotropic mode, as is commonly assumed, unless appropriate conditions such as basic state  
458 shear occur in the regions of descent. Furthermore, for interhemispheric teleconnections or  
459 tropical to mid-latitude teleconnections, the first leg of the teleconnection occurs in the baroclinic  
460 mode. Equatorially trapped baroclinic waves can be responsible for most of the propagation  
461 within regions where low-frequency barotropic modes are evanescent, including across the  
462 equator. Diagnosis of interaction terms as a forcing in the barotropic equation in the QTCM

463 results then allows us to identify the relative importance of each mechanism in exciting the  
464 barotropic mode: the shear advection mechanism, the surface drag mechanism and the vertical  
465 advection mechanism. In these results, the Rossby wave source in the barotropic equation due to  
466 shear advection roughly coincides with the baroclinic signal in the tropics and subtropics, and  
467 thus can be effective in contributing to the southern hemisphere response to an Atlantic Warm  
468 Pool heat source. The barotropic Rossby wave source due to surface drag is more broadly  
469 spatially spread, essentially reflecting the contribution of the baroclinic mode to low-level wind,  
470 and has large enough magnitude to provide a substantial forcing mechanism for interhemispheric  
471 teleconnections. Last, the barotropic Rossby wave source due to vertical advection is significant  
472 in locations where the climatological vertical velocity and vertical shear are both large. These  
473 mechanisms were further examined by modifying the simple model to include the surface drag  
474 and vertical advection one by one, and by comparing their effects with the shear advection  
475 mechanism. The results from the simple model provide support to the interpretation of QTCM  
476 results.

477         The QTCM results also allowed for an assessment of effects that moist feedbacks can  
478 have in such interhemispheric teleconnections. Moist processes strengthen the initial heating  
479 locally. In the Atlantic Warm Pool experiment, the region of anomalous heating is extended  
480 westward by the induced precipitation anomalies in the Eastern Pacific ITCZ region. This  
481 amplifies the original teleconnection response, as shown if these anomalies are applied  
482 separately. Such an effect depends on the regional basic state: it does not occur for a similar  
483 initial anomaly applied in the central Pacific. Additional moist feedbacks can occur remotely. In  
484 the Atlantic warm pool experiment, induced precipitation anomalies are obtained in both the  
485 equatorial Western Pacific and the subtropical Eastern Pacific. The latter contribute to the



486 vertical advection forcing of barotropic motions in the southern hemisphere. The total moist  
487 feedback on the teleconnection process is thus able to alter significantly the teleconnection  
488 response to tropical heating.

489

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494

## 495 APPENDIX

### 496 QTCM equations

497 QTCM is a nonlinear tropical circulation model that makes use of constraints from a  
498 particular QE convective scheme, the Betts-Miller scheme, but does not assume that convective  
499 QE has to hold. To achieve this, temperature, velocity and moisture are expanded in terms of a  
500 truncated series of basis functions in the vertical:

$$501 \quad T = T_r(p) + \sum_{k=1}^K a_k(p) T_k(x, y, t) \quad (\text{A1})$$

$$502 \quad \mathbf{v} = \sum_{k=0}^L V_k(p) \mathbf{v}_k(x, y, t) \quad (\text{A2})$$

$$503 \quad q = q_r(p) + \sum_{k=1}^K b_k(p) q_k(x, y, t) \quad (\text{A3})$$

504 The model simply takes analytical solutions that hold approximately under QE conditions and  
 505 employs them as leading basis functions to represent the vertical structure of the flow.

506 For the standard version of QTCM1, a single deep convective mode is retained in the  
 507 vertical thermodynamic structure (i.e.,  $T = T_r(p) + a_1(p)T_1(x, y, t)$ ) with two components (barotropic  
 508  $V_0(p)$  and baroclinic  $V_1(p)$ ) in the vertical structure of velocity. Discretization of the moisture  
 509 equation is largely independent. The model simply chooses a truncation for the moisture  
 510 equation to have a similar level of complexity as for the temperature equation.

511 Using  $V_0$  and  $V_1$  as the basis functions, the momentum equations are projected onto these  
 512 (i.e., taking the inner product of the momentum equation with  $V_0$  and  $V_1$  respectively) to obtain  
 513 the prognostic equations for barotropic wind component and baroclinic wind component:

$$514 \quad \partial_t \zeta_0 + \text{curl}_z(\mathcal{D}_{V_0}(\mathbf{v}_0, \mathbf{v}_1)) + \beta v_0 = -\text{curl}_z(\varepsilon_0 \mathbf{v}_0) - \text{curl}_z(\varepsilon_{10} \mathbf{v}_1) \quad (\text{A4})$$

$$515 \quad \partial_t \mathbf{v}_1 + \mathcal{D}_{V_1}(\mathbf{v}_0, \mathbf{v}_1) + \mathbf{f} \mathbf{k} \times \mathbf{v}_1 = -\kappa \nabla T_1 - \varepsilon_1 \mathbf{v}_1 - \varepsilon_{01} \mathbf{v}_0 \quad (\text{A5})$$

516 where the advection-diffusion operators are given by:

$$517 \quad \mathcal{D}_{V_0}(\mathbf{v}_0, \mathbf{v}_1) = \mathbf{v}_0 \cdot \nabla \mathbf{v}_0 + \langle V_1^2 \rangle \mathbf{v}_1 \cdot \nabla \mathbf{v}_1 + \langle V_1^2 \rangle (\nabla \cdot \mathbf{v}_1) \mathbf{v}_1 - K_H \nabla^2 \mathbf{v}_0 \quad (\text{A6})$$

$$518 \quad \mathcal{D}_{V_1}(\mathbf{v}_0, \mathbf{v}_1) = \mathbf{v}_0 \cdot \nabla \mathbf{v}_1 + \frac{\langle V_1^3 \rangle}{\langle V_1^2 \rangle} \mathbf{v}_1 \cdot \nabla \mathbf{v}_1 + \mathbf{v}_1 \cdot \nabla \mathbf{v}_0 - \left( \langle V_1 \Omega_1 \partial_p V_1 \rangle / \langle V_1^2 \rangle \right) (\nabla \cdot \mathbf{v}_1) \mathbf{v}_1 - K_H \nabla^2 \mathbf{v}_1 \quad (\text{A7})$$

519 vertical averages over the troposphere are defined as:

$$520 \quad \hat{X} = \langle X \rangle = p_T^{-1} \int_{p_n}^{p_n} X dp \quad (\text{A8})$$

521 and  $\Omega_1(p)$  represents the vertical structure of vertical velocity from the baroclinic wind. Because  
 522 vertical velocity is diagnostic in the primitive equations, solving the continuity equation gives:

523 
$$\omega_1(x, y, p, t) = -\Omega_1(p) \nabla \cdot \mathbf{v}_1(x, y, t) \quad (\text{A9})$$

524 
$$\text{and } \Omega_1(p) = -\int_p^{p_s} V_1(p) dp \quad (\text{A10})$$

525 Two of the terms arising from vertical transfer of momentum to surface stress by parameterized  
 526 subgrid-scale turbulence in the barotropic equation are defined as:

527 
$$\varepsilon_0 = (g / p_T) \rho_a C_D V_s \quad (\text{A11})$$

528 
$$\varepsilon_{10} = (g / p_T) \rho_a C_D V_s V_{1s} \quad (\text{A12})$$

529 where  $V_s$  is calculated as  $\sqrt{u_s^2 + v_s^2 + V_{s\min}^2}$ , and  $V_{1s}$  is value of the baroclinic basis function  $v_1$  at  
 530 surface. The surface drag coefficient  $C_D$  changes according to land surface type. The sign of  $\varepsilon_0$   
 531 and  $\varepsilon_{10}$  are set as opposite in the model in order that the two surface drag terms has the same  
 532 form.

533 Vertically integrating the temperature and moisture equations from the standard nonlinear  
 534 primitive equations, with vertical velocity and velocity truncated at  $V_1$  yields:

535 
$$\hat{a}_1(\partial_t + \mathcal{D}_{T1})T_1 + M_{s1} \nabla \cdot \mathbf{v}_1 = \langle Q_c \rangle + (g / p_T) \times (-R_t^\uparrow - R_s^\downarrow + R_s^\uparrow + S_t - S_s + H) \quad (\text{A13})$$

536 
$$\hat{b}_1(\partial_t + \mathcal{D}_{q1})q_1 + M_{q1} \nabla \cdot \mathbf{v}_1 = \langle Q_q \rangle + (g / p_T) E \quad (\text{A14})$$

537 where the advection-diffusion operators are, respectively:

538 
$$\mathcal{D}_{T1} = \mathbf{v}_0 \cdot \nabla + \hat{a}_1^{-1} \langle a_1 V_1 \rangle \mathbf{v}_1 \cdot \nabla - K_H \nabla^2 \quad (\text{A15})$$

539 
$$\mathcal{D}_{q1} = \mathbf{v}_0 \cdot \nabla + \hat{b}_1^{-1} \langle b_1 V_1 \rangle \mathbf{v}_1 \cdot \nabla - K_H \nabla^2 \quad (\text{A16})$$

540 and the dry static stability  $M_{s1}$  and the gross moisture stratification  $M_{q1}$  are given by, respectively:

541 
$$M_{s1} = p_T^{-1} \int_{p_n}^{p_s} \Omega_1(-\partial_p s) dp \quad (\text{A17})$$

542 
$$M_{q1} = p_T^{-1} \int_{p_n}^{p_s} \Omega_1(-\partial_p q) dp \quad (\text{A18})$$

543 where  $s = T + \phi$  is the dry static energy, with  $\phi$  the geopotential. The moist convective  
 544 parameterization projects the Betts – Miller scheme onto the basis functions of temperature and  
 545 moisture, resulting in:

546 
$$\langle Q_c \rangle = -\langle Q_q \rangle = \varepsilon_c^* (q_1 - T_1) \quad (\text{A19})$$

547 where  $\varepsilon_c^* \equiv \hat{a}_1 \hat{b}_1 (\hat{a}_1 + \hat{b}_1)^{-1} \varepsilon_c$  and  $\varepsilon_c = \tau_c^{-1} \mathcal{H}(C_1)$ , with  $\tau_c$  the convective adjustment time,  $\mathcal{H}(C_1)$  a  
 548 Heaviside function that represents the dependence of convection on conditional instability in the  
 549 column, and  $C_1$  a measure of CAPE for this model. Detailed treatment and parameterization of  
 550 other terms on the right hand side of the temperature and moisture equations can be found in  
 551 Neelin and Zeng (2000).

552

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## 643 **List of Figures**

644 FIG. 1. (a) The Gaussian-shaped baroclinic heating anomaly prescribed in the Atlantic Warm  
645 Pool region in QTCM, the amplitude at the center (20°N, 70°W) is equivalent to 6mm/day of  
646 precipitation (i.e., 169.2W/m<sup>2</sup>). (b) The precipitation anomalies in QTCM AWP experiment,  
647 negative contour lines are dashed. The contour intervals in both are 1mm/day (the 0.5mm/day  
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649 FIG. 2. The baroclinic streamfunction anomalies (a) and barotropic streamfunction anomalies (b)  
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652 FIG. 3. The three forcing sources in the QTCM AWP experiment: (a) shear advection; (b)  
653 surface drag; (c) vertical advection; and (d) v1 component of the surface drag (see text for  
654 explanation). Negative contour lines are dashed. The contour intervals are  $2 \times 10^{-12} \text{ s}^{-2}$  within  
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658 shear advection; (b) surface drag; (c) vertical advection. Negative contour lines are dashed. The  
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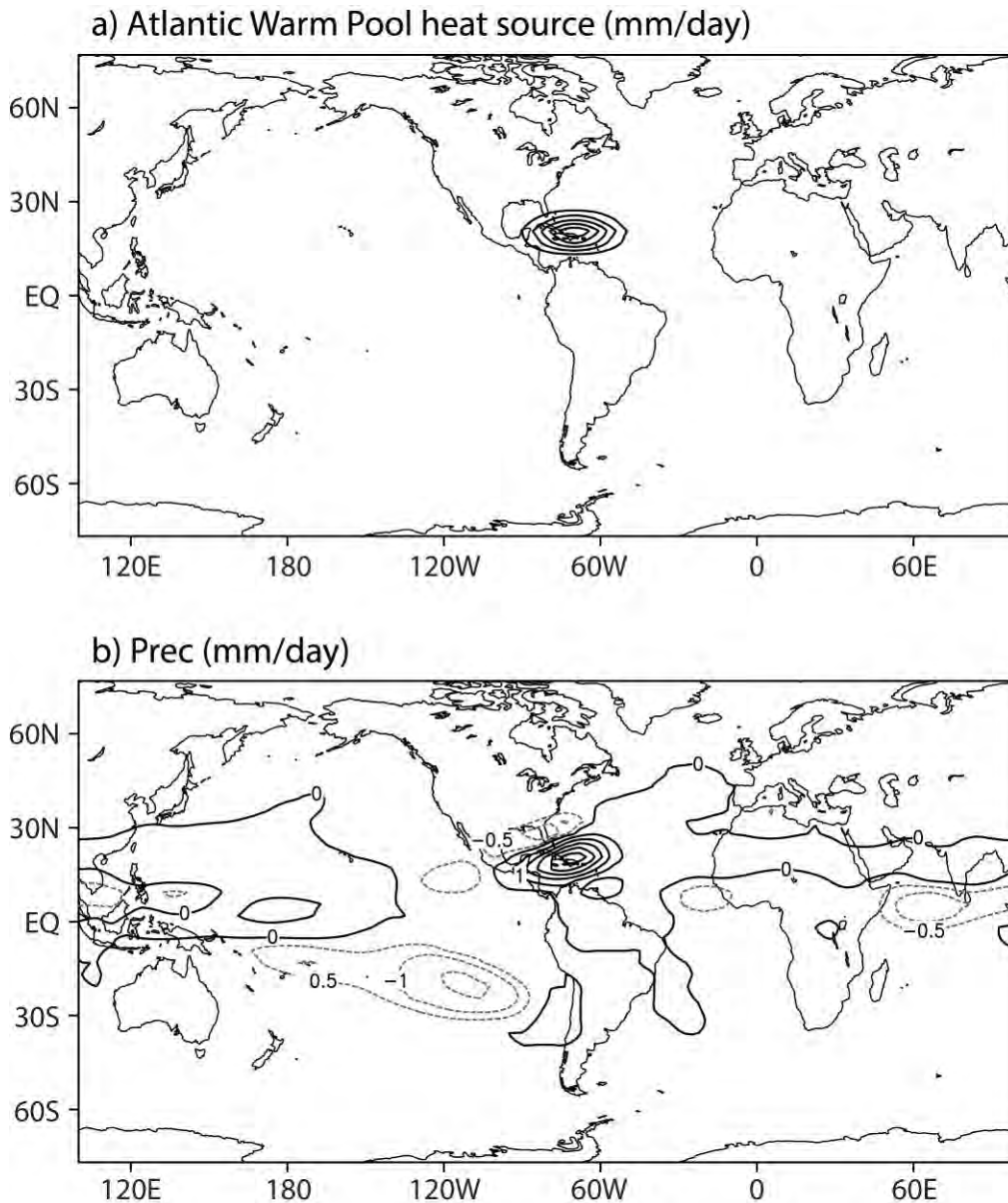
662 FIG. 5. The barotropic streamfunction anomalies in the Eastern Pacific experiment in QTCM.  
663 Negative contour lines are dashed. The contour interval is  $2 \times 10^5 \text{ m}^2 \text{ s}^{-1}$ . The shaded area is the  
664 heating prescribed in the eastern Pacific, with interval 1mm/day.

665 FIG. 6. (a) As in Fig. 1a, except shifting the heat source  $90^\circ$  in longitude to the central Pacific  
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671 FIG. 8. The barotropic streamfunctions anomalies in the simple model AWP experiment (a) with  
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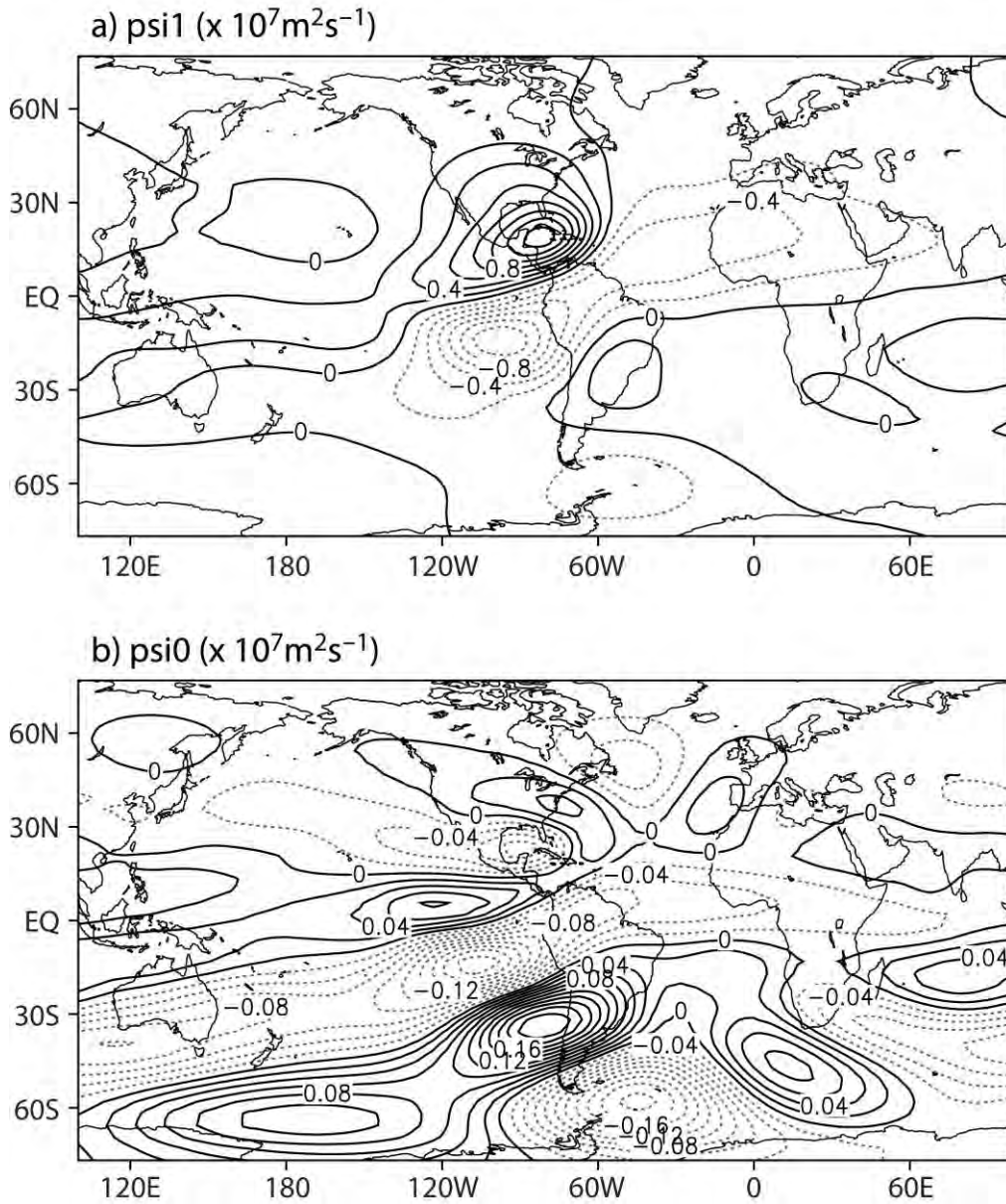
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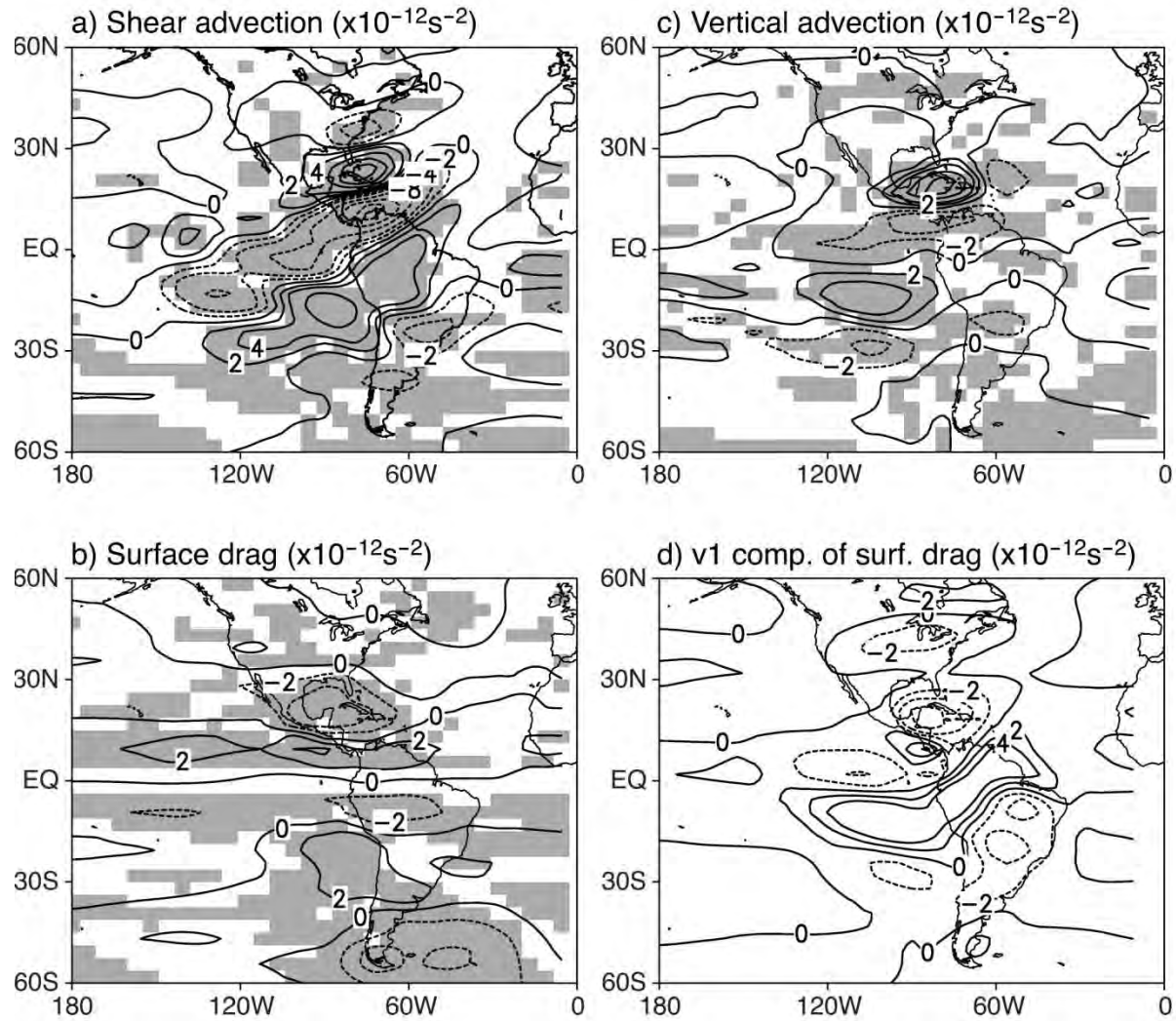


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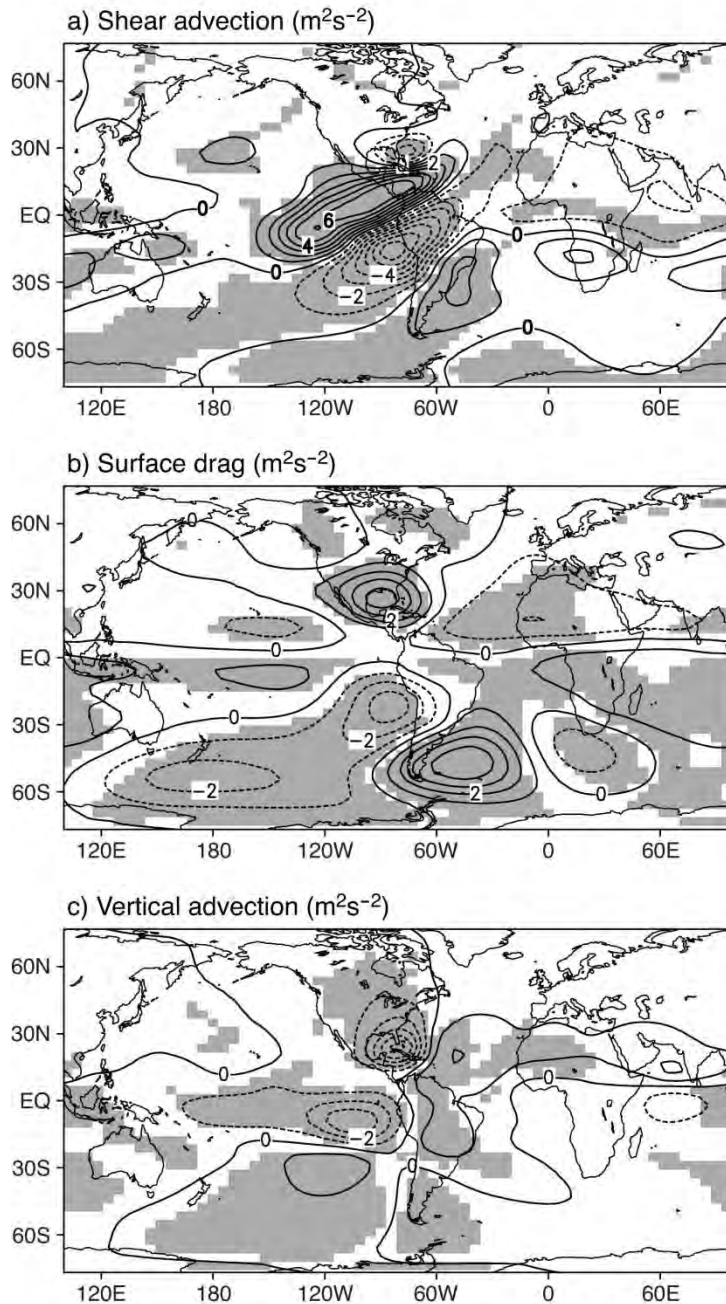


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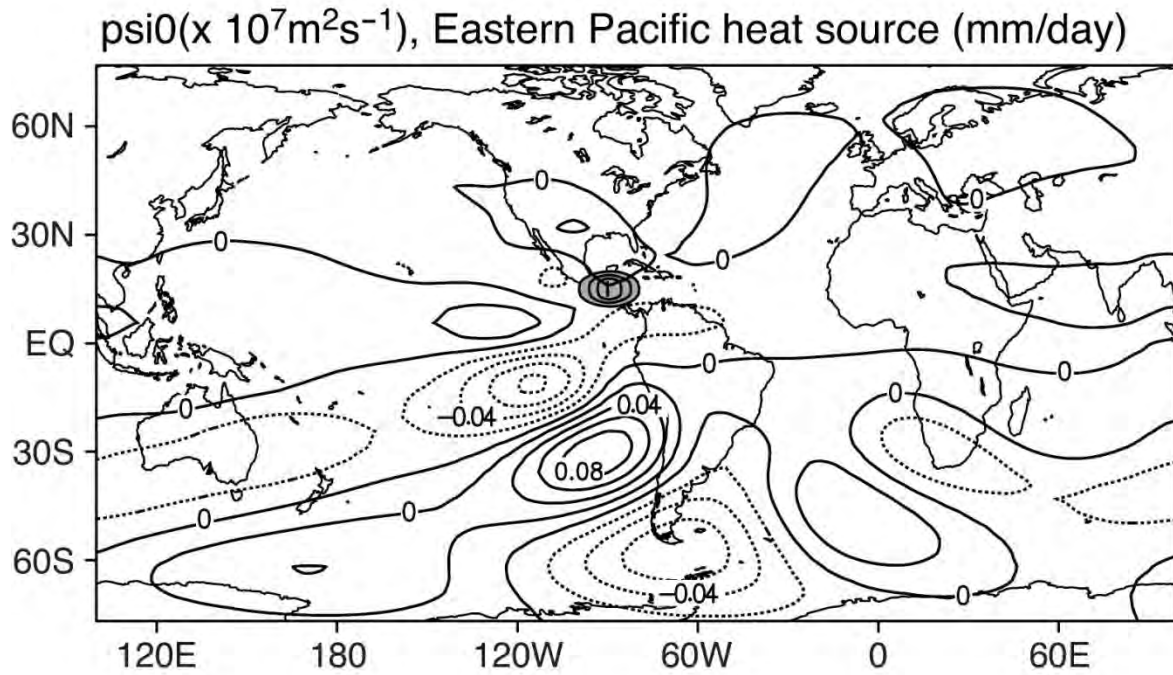
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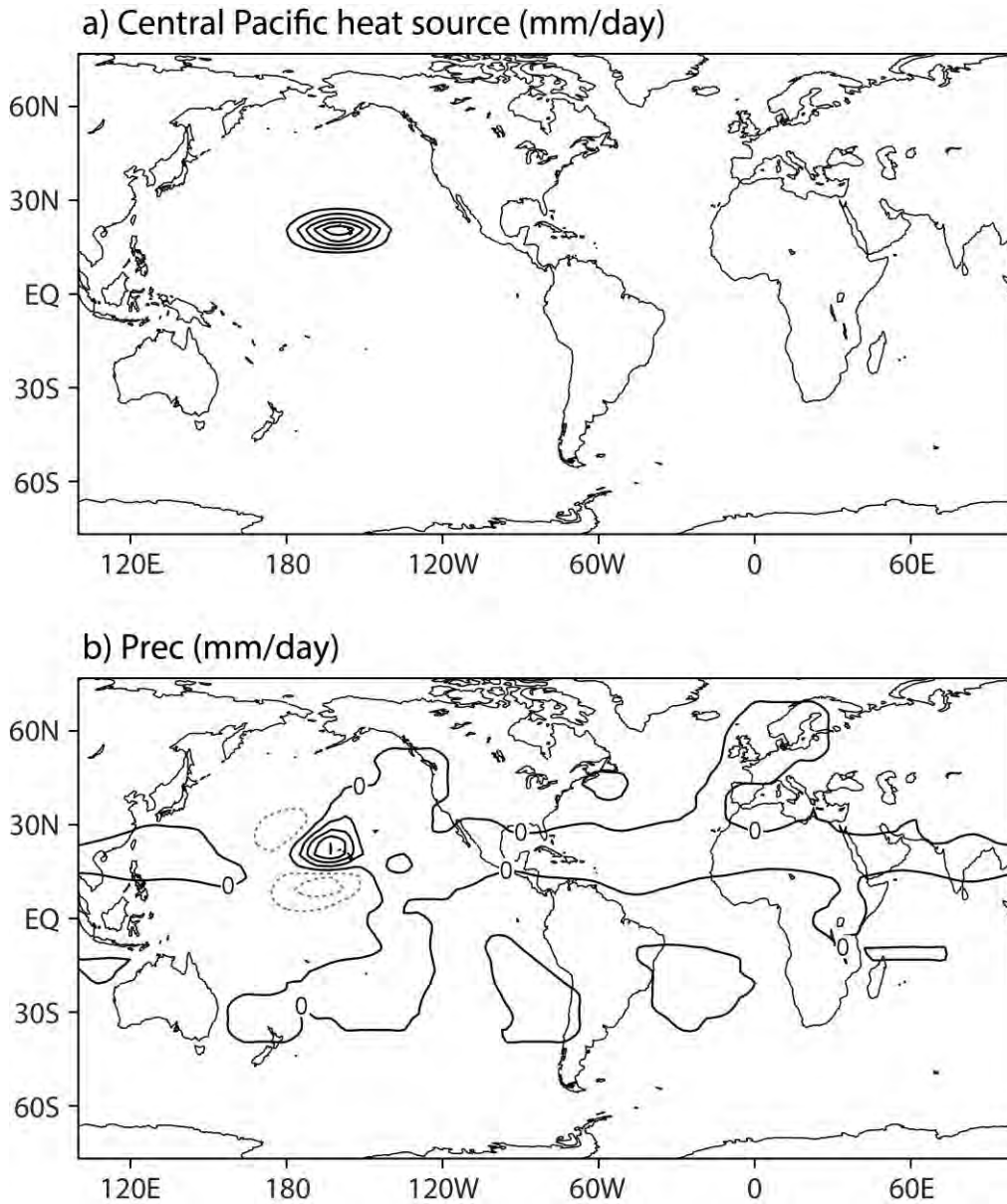
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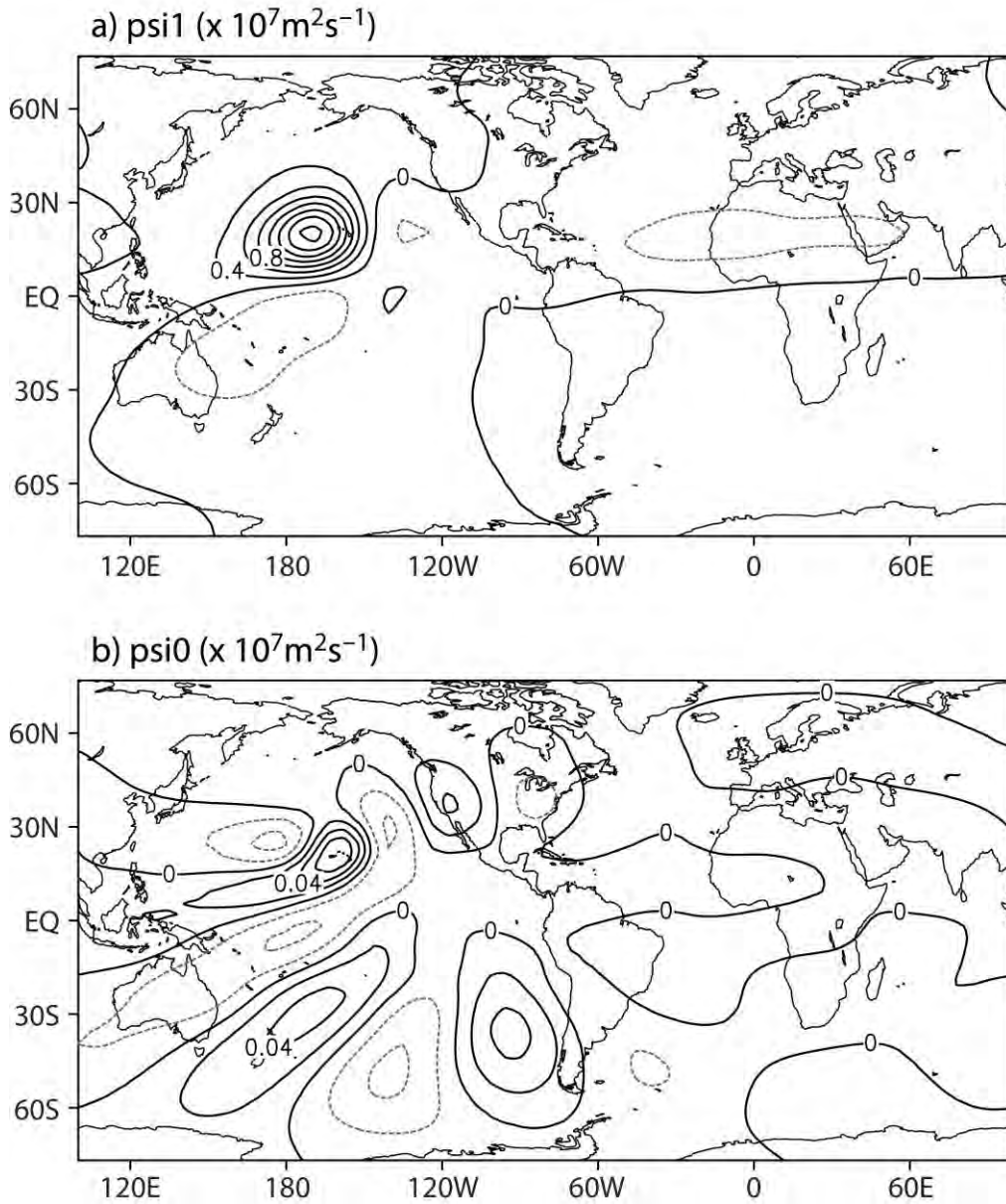
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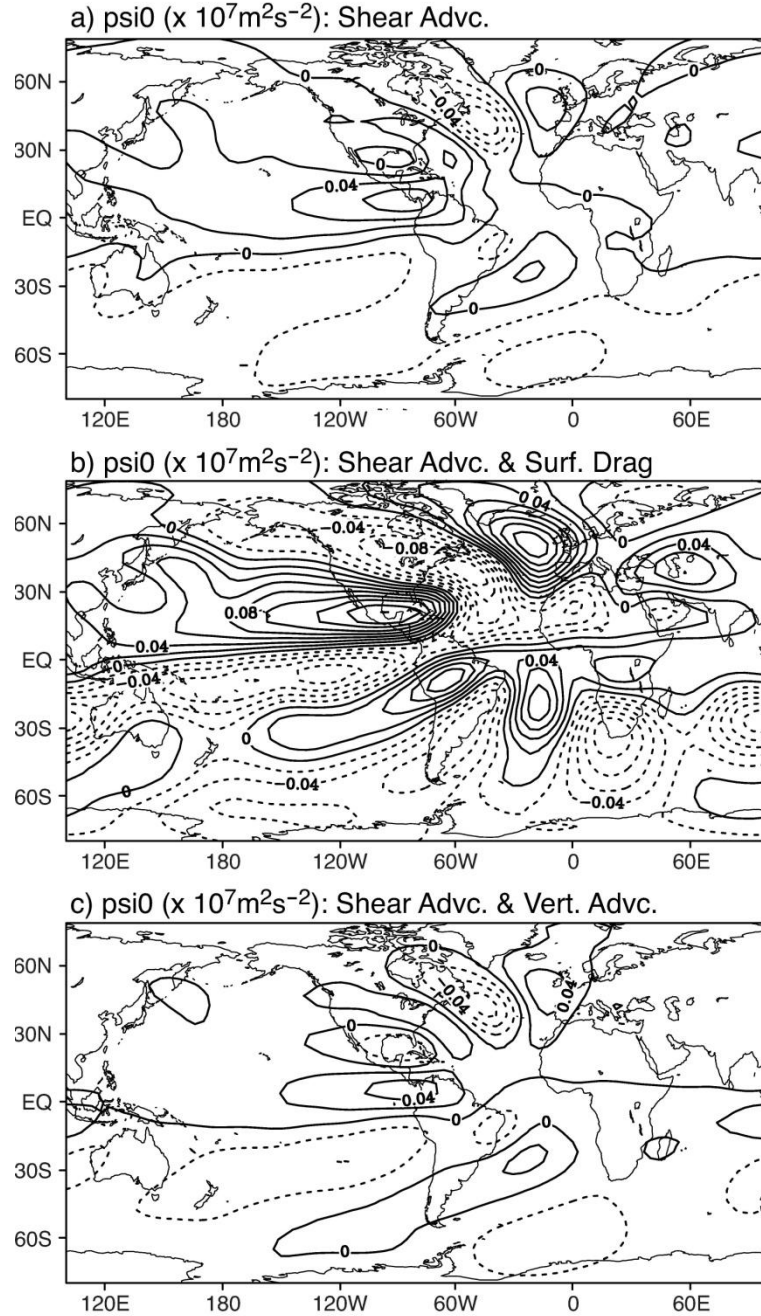




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